



POTSDAM INSTITUTE FOR  
CLIMATE IMPACT RESEARCH

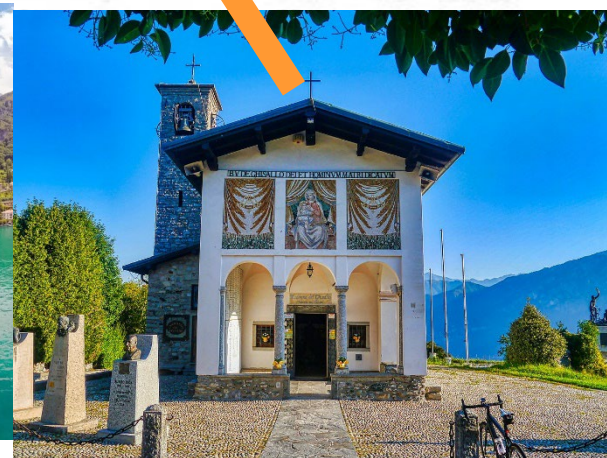
# Energy System Models

NAVIGATE-ENGAGE Summer School,  
Como, Italy, July 3-7, 2023

Nico Bauer, Potsdam Institute for Climate Impact Research (PIK), Germany, @NB\_pik



# Overview of the lecture



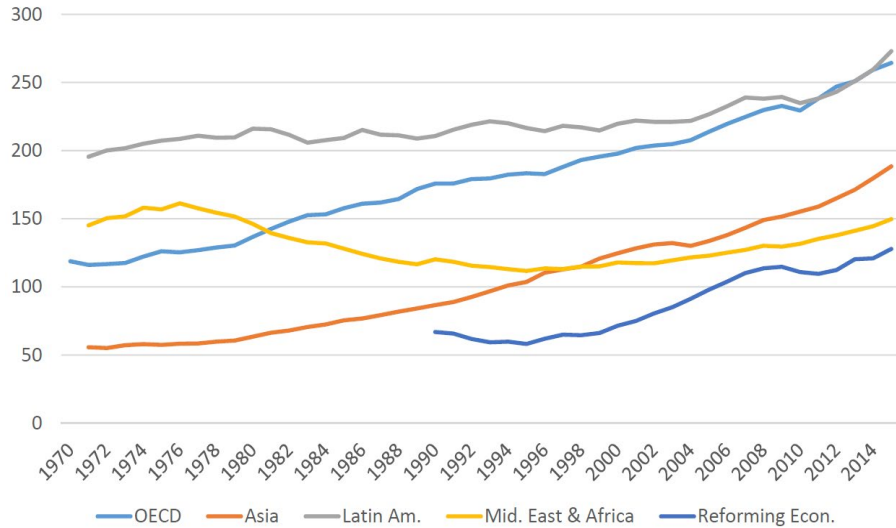
# Introduction

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- Energy, economy and environment
- General structure of energy system models
- Mathematical structure of a Energy System Models
  - Partial equilibrium models: Linear programming
  - Going non-linear: demands, mixes, capacity ramp-up
  - General equilibrium models: Coupling to economy model
- Applications
  - Political economy: Fossil fuel markets and climate policy
  - Endogenous technological change: the learning curve approach
  - Issue linkage: air pollution and public health

# Introduction – International inequality and climate policies

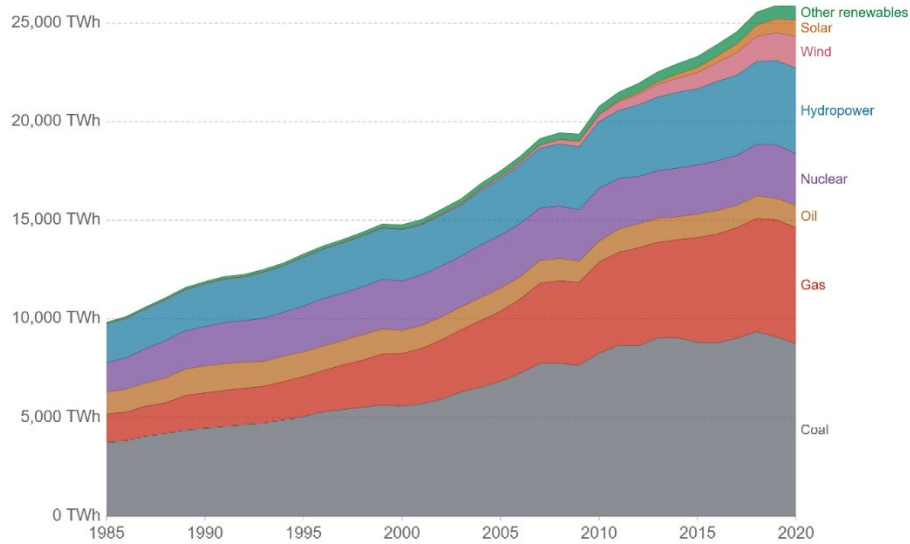
Final energy productivity in US\$ per GJ



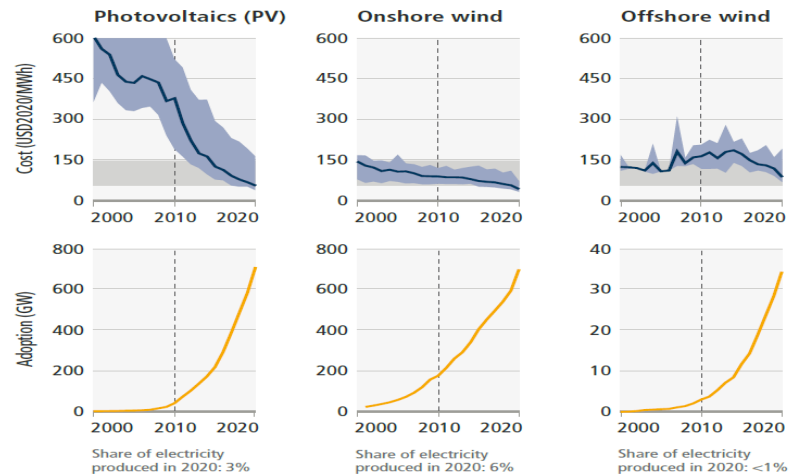
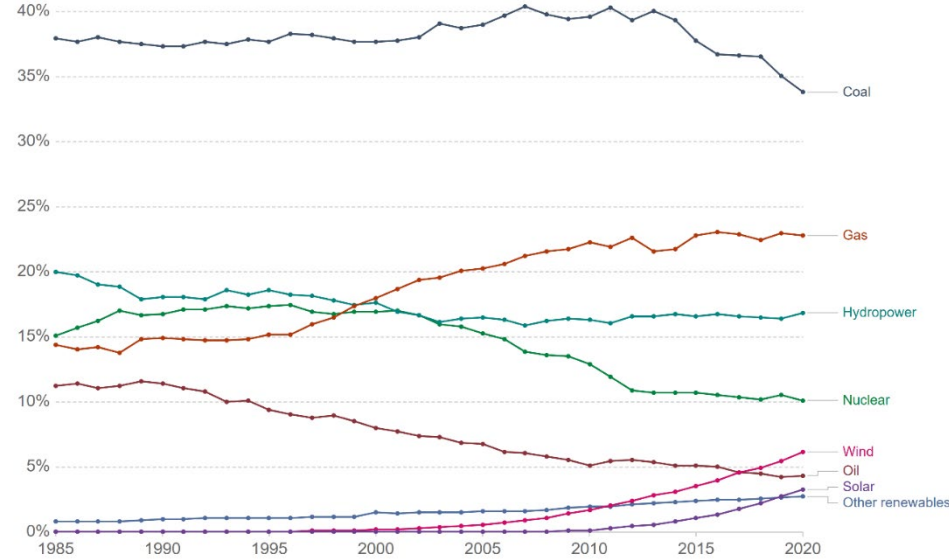
- OECD countries have high per-capita incomes
- ... high CO<sub>2</sub> emissions per capita
- ... high carbon productivity
- ... high energy productivity
  
- Climate change is a global commons good problem
- Each ton of CO<sub>2</sub> is equal

# Some basics about electricity

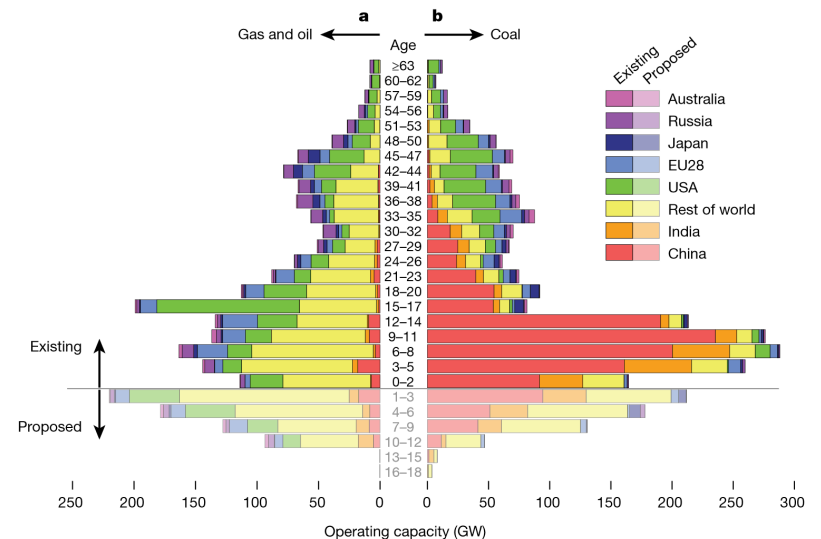
Electricity production by source, World



Share of electricity production by source, World



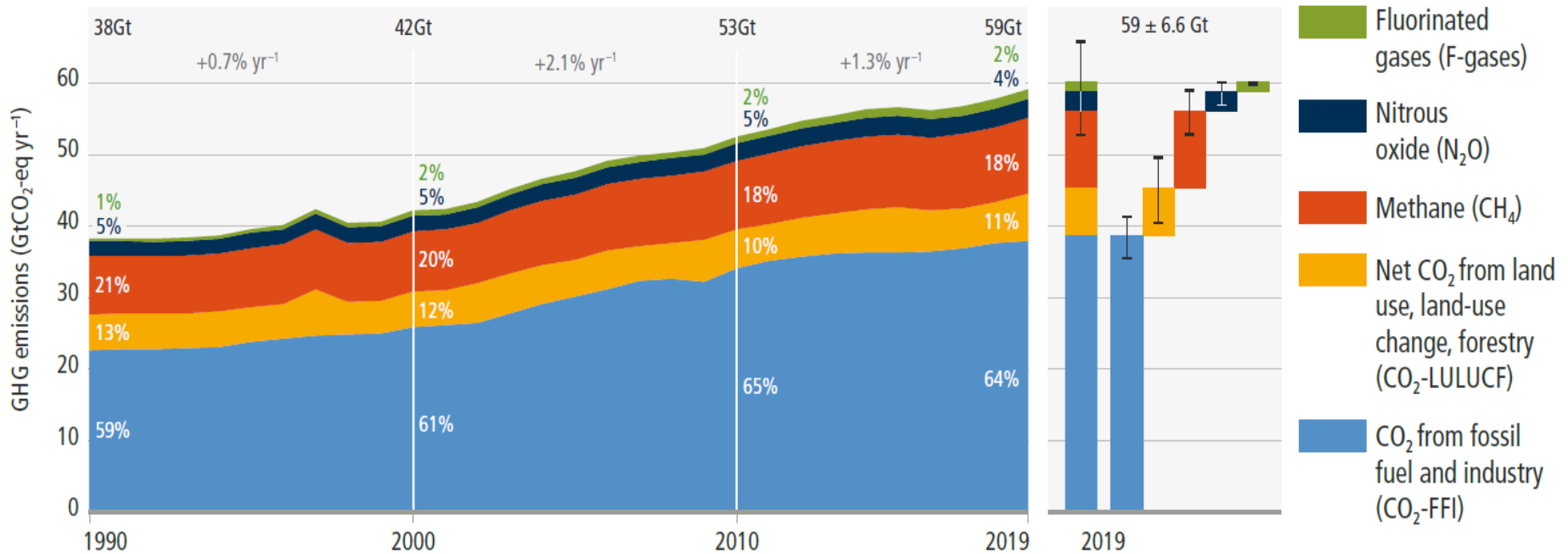
— Market cost  
— Adoption (note different scales)  
--- AR5 (2010)  
■ Fossil fuel cost (2020)





# Global GHG emissions

a. Global net anthropogenic GHG emissions 1990–2019<sup>(5)</sup>



IPCC AR6 WG3 SPM Fig. SPM 1

# Global CO2 Emissions – Fossil Fuels

- Emissions are not measured directly
- Human activities related to emissions are measured (tax authorities, etc.) and multiplied by emission factors
- What are the annual CO2 emissions from fossil fuels?
- Activity: Annual fossil fuel combustion → unit EJ/yr
- Emission factor: GtCO2/EJ
- BP energy statistics for 2021: 33.884 GtCO2

		Coal	Oil	Gas	Total
Consumption	EJ/yr	160.1	184.2	145.3	489.6
Carbon Intensity	MtCO2/EJ	95	73	55	
Emissions	GtCO2/yr	15.3	13.5	8.0	36.8

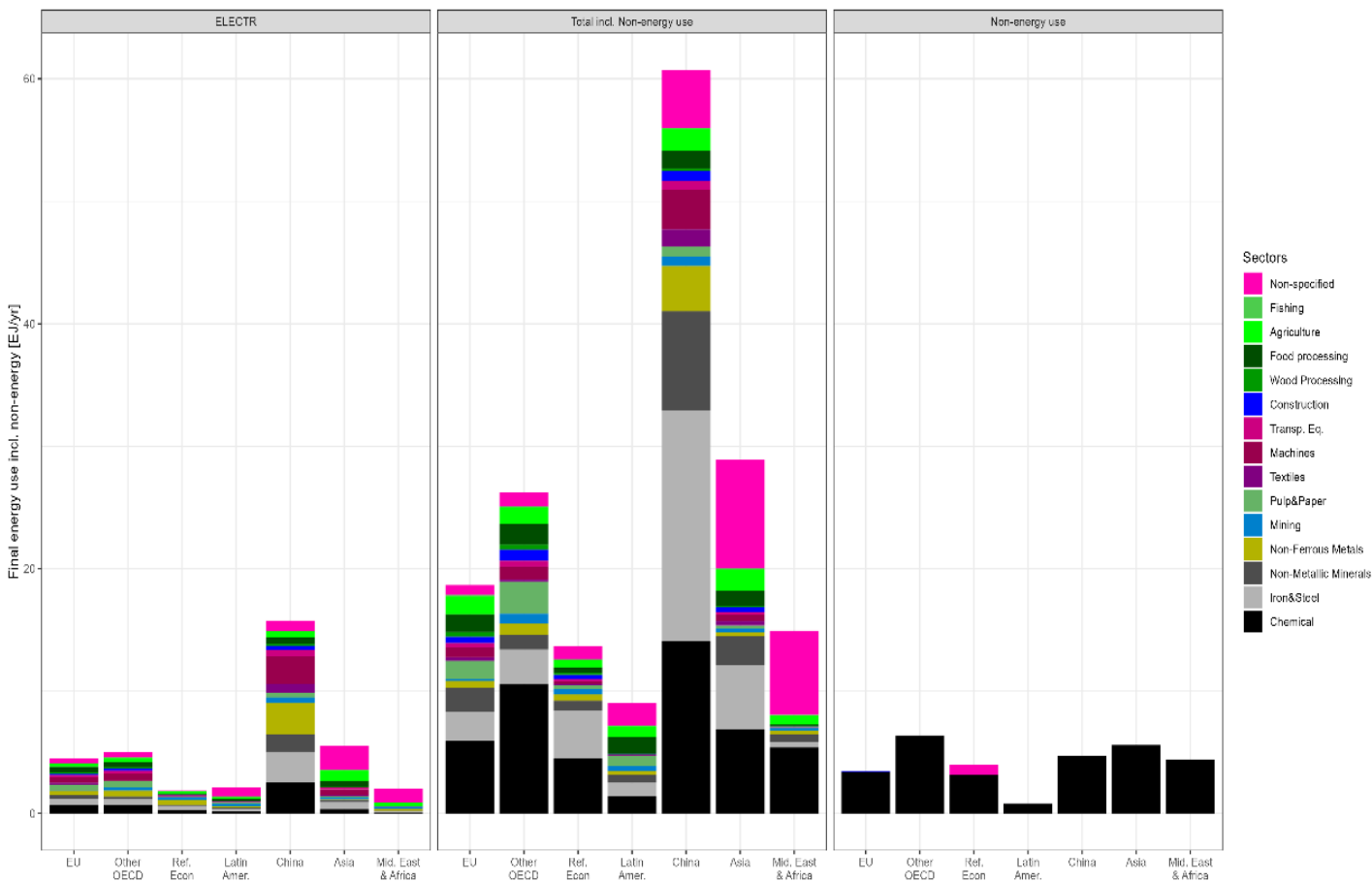
- Why the difference?

# Fossil fuels are not only used for energy, but also in industry

## Electricity

## All Energy

## Non-Energy Use





# Making different GHGs comparable

	Unit	CO <sub>2</sub>	CH <sub>4</sub>	N <sub>2</sub> O
Atmospheric lifetime	Years	~150	12	114
GWP20	Ton/Ton	1	84	265
GWP100	Ton/Ton	1	28	298
GWP500	Ton/Ton	1	7	156
Emissions 2010		31.7Gt	330Mt	10.5Mt
Emissions 2010 GWP100	GtCO <sub>2</sub> -eq	31.7	9.2	3.1

- Parameters defining GWP (lifetime and radiative forcing) are uncertain
- Choice of GWP is political and depends on the time-horizon
- CH<sub>4</sub> reacts strongly with O<sub>2</sub>
- Some countries have higher CH<sub>4</sub> emissions than others
- USA from gas, China from coal

# Linear Programming – The standard form (of the primal)

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$$\text{Min } C = \sum_{i,j} c_{i,j} x_{i,j}$$

Subject to

$$\text{Final energy demand} \quad D_j \leq \sum_i a_{i,j} x_{i,j} \quad \forall j$$

$$\text{Primary energy resource} \quad R_i \geq \sum_j x_{i,j} \quad \forall i$$

$$\text{Non-negativity} \quad x_{i,j} \geq 0 \quad \forall i, j$$

$c_{i,j}$  cost coefficients

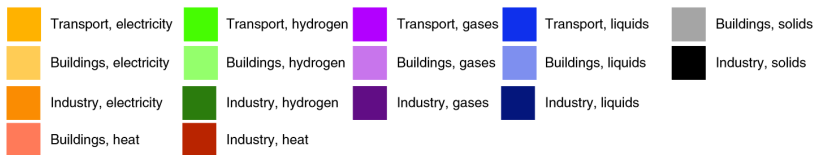
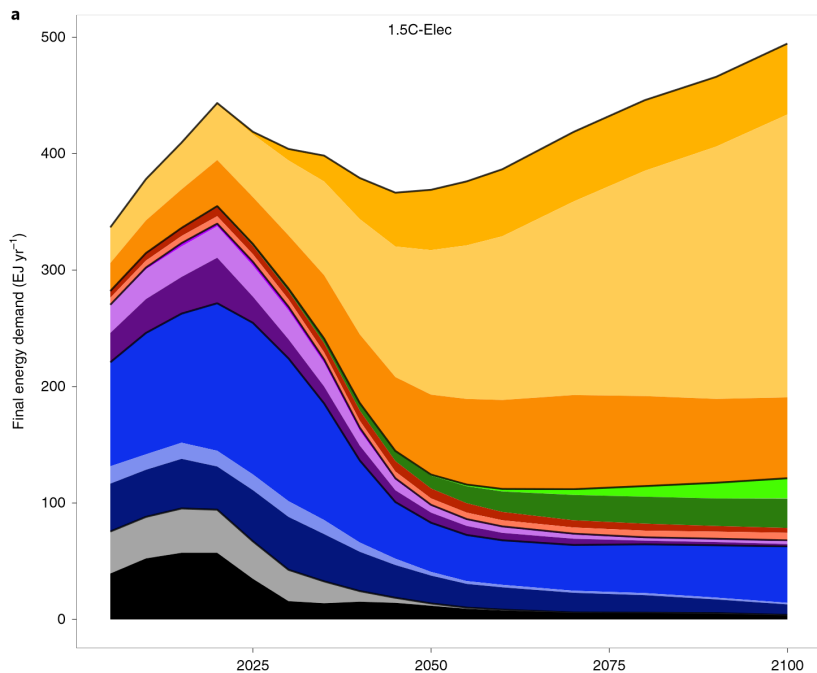
$x_{i,j}$  activity variables (primal variables)

$a_{i,j}$  conversion factors

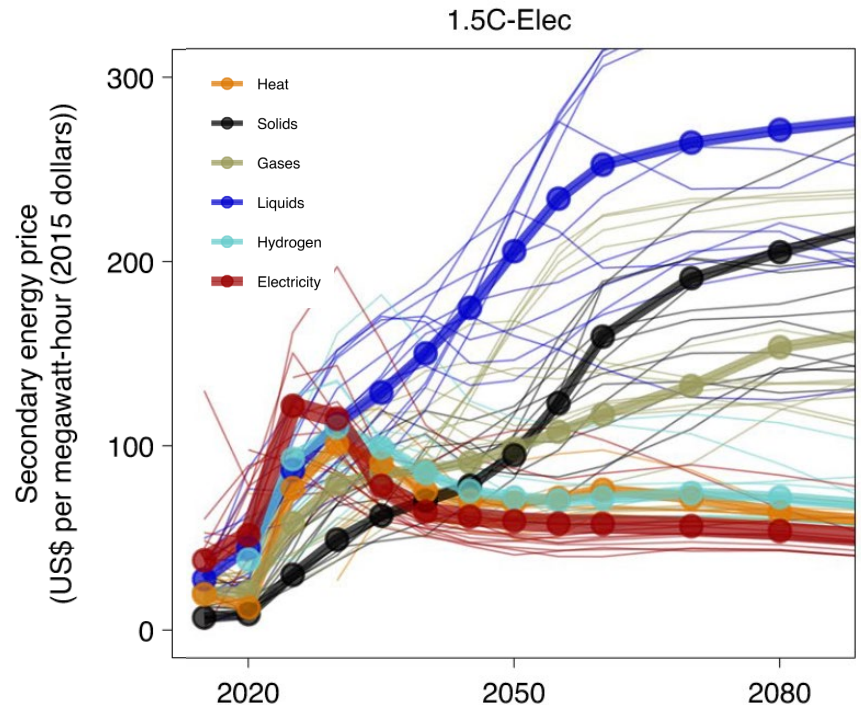
# Linear Programming – Optimal solution

- Solution algorithm: Simplex algorithm finds set of  $x_{i,j}$  that minimizes C
- Some inequalities are binding, but not necessarily all
- Each constraint has a dual variable → shadow price
- The following complementarities hold for the inequalities
  - $\delta_j (D_j - \sum_j a_{i,j} x_{i,j}) = 0 \quad \forall j$  Final energy price
  - $\rho_i (R_i - \sum_i x_{i,j}) = 0 \quad \forall i$  Primary energy price
  - $\omega_{i,j} x_{i,j} = 0 \quad \forall i, j$  Subsidy to push  $x_{i,j}$  into the market

# A simple example



Luderer et al. (2021) <https://www.nature.com/articles/s41560-021-00937-z>



Note: this is for illustrative purposes. It is based on the REMIND-Model that represents price-responsive demands and energy substitution. This will come latter

# Linear programming – Interpretation of results

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- There is an optimal solution only if the problem is feasible  
→ constraints define a non-empty set
- The solution is unique!
- Symmetry between
  - Centralized planner problem → benevolent dictator → shadow prices
  - Decentralized market solution → “invisible hand” of the market → market prices
- Pre-condition is the competitive market equilibrium
  - Atomistic actors that cannot influence the price
  - Full information on all technologies (no info-asymmetry)
  - No market entry and exit barriers;
  - marginal quantity changes, no ramp-up costs, unit commitments
  - No transaction costs
  - Optimal solutions can still induce external effects like air pollution, but if there is no feedback
  - [Since the model is static – so far – we need not say anything about dynamic imperfections and expectation formation]

# Linear Programming – A powerful modeling tool

$$\text{Min } C = \sum_{i,j} c_{i,j} x_{i,j}$$

Subject to

$$\text{Final energy demand} \quad D_j \leq \sum_j a_{i,j} x_{i,j} \quad \forall j$$

$$\text{Primary energy resource} \quad R_i \geq \sum_i x_{i,j} \quad \forall i$$

$$\text{Non-negativity} \quad x_{i,j} \geq 0 \quad \forall i,j$$

$c_{i,j}$  cost coefficients

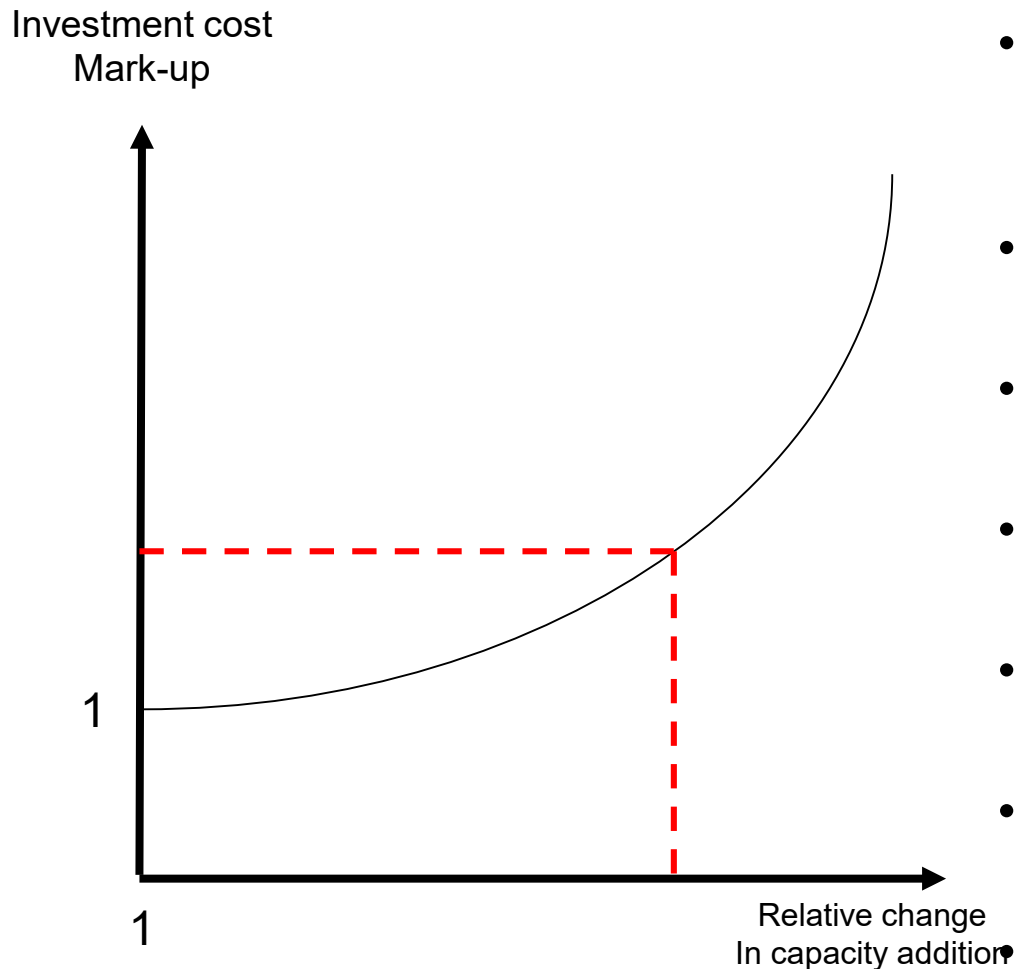
$x_{i,j}$  activity variables (primal variables)

$a_{i,j}$  conversion factors

## Discussion

- Emissions included via emission factors
- Dynamics can be added:
  - Exhaustible resources
  - Capacities
  - Constraints on changes
  - Changes of tech. and cost parameters (as long as no non-linearity is introduced)
- Locations, transport, net-works
- Not only energy: food, water, materials, ...
- Behavioural factors can be included
- We can analyze a broad set of policies
- Information and data demanding method
- Sensitive behaviour due to linear structure
- Many constraints are added, with little empirical basis
- Very difficult to calibrate
  - Optimal solution usually deviates from statistics
  - Replication of data requires inclusion of more processes and policies and constraints

# Going non-linear – Adjustment costs



- Capacity ramp-up can be very, very rapid, if investment costs are constant
  - Hard growth constraints lead to numerical issues
  - Adjustment costs are soft-constraints
  - Investment costs increase, if capacity additions accelerate
  - Build the capacity to build capacities
  - Can be interpreted as a dynamic supply function
- Expectations & early investments

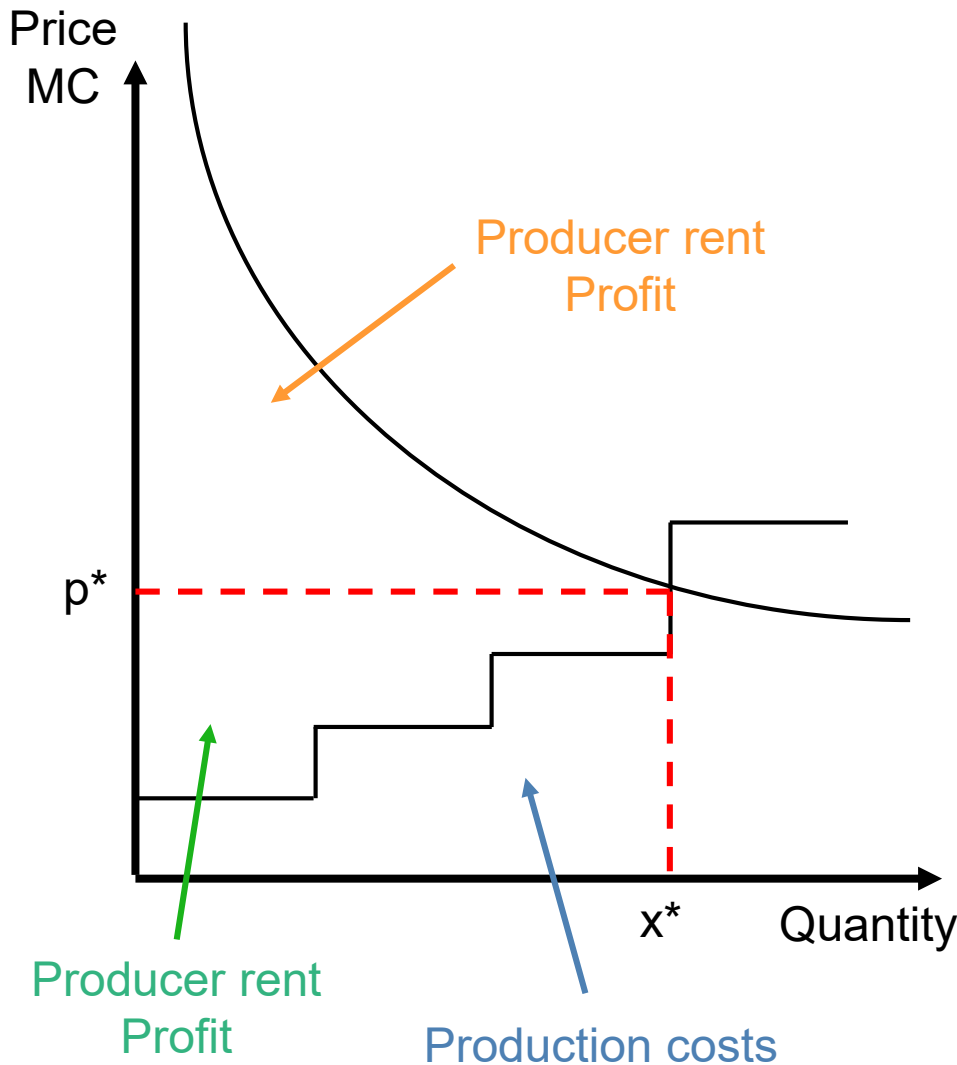


# Going non-linear – Discrete Choice Models

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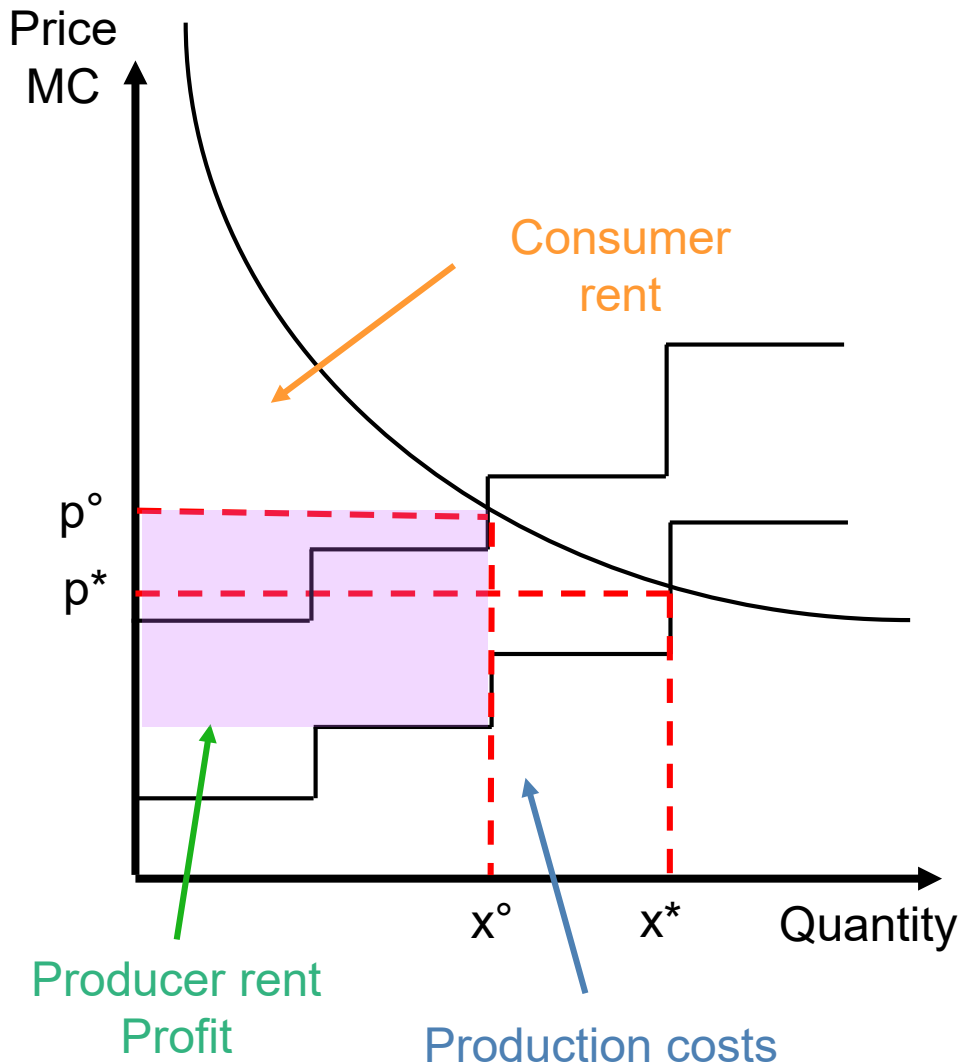
- Addresses radical shifts in technology mix typical for LP (flip-flop, bang-bang, penny-switching, ...)
- Approach: discrete choice models (e.g. multinomial logit)
- Choice probability  $i$  chooses  $n$ : 
$$P_{n,i} = \frac{\exp(\beta c_{n,i})}{\sum_{j=1}^J \exp(\beta c_{n,j})}$$
 characteristics of individual  $i$  and alternative  $n$  (e.g. price)
- Data for calibration: shares (e.g. modal split in transport)
- $P_{n,i}$  is constant, if  $c_{n,i}$  even under growing scale
- Changes in prices shift the mix gradually, while total demand is fulfilled

# Going non-linear – Price-responsive demands



- Demand function is calibrated to replicate the demand level
- Revenue = cost + profit

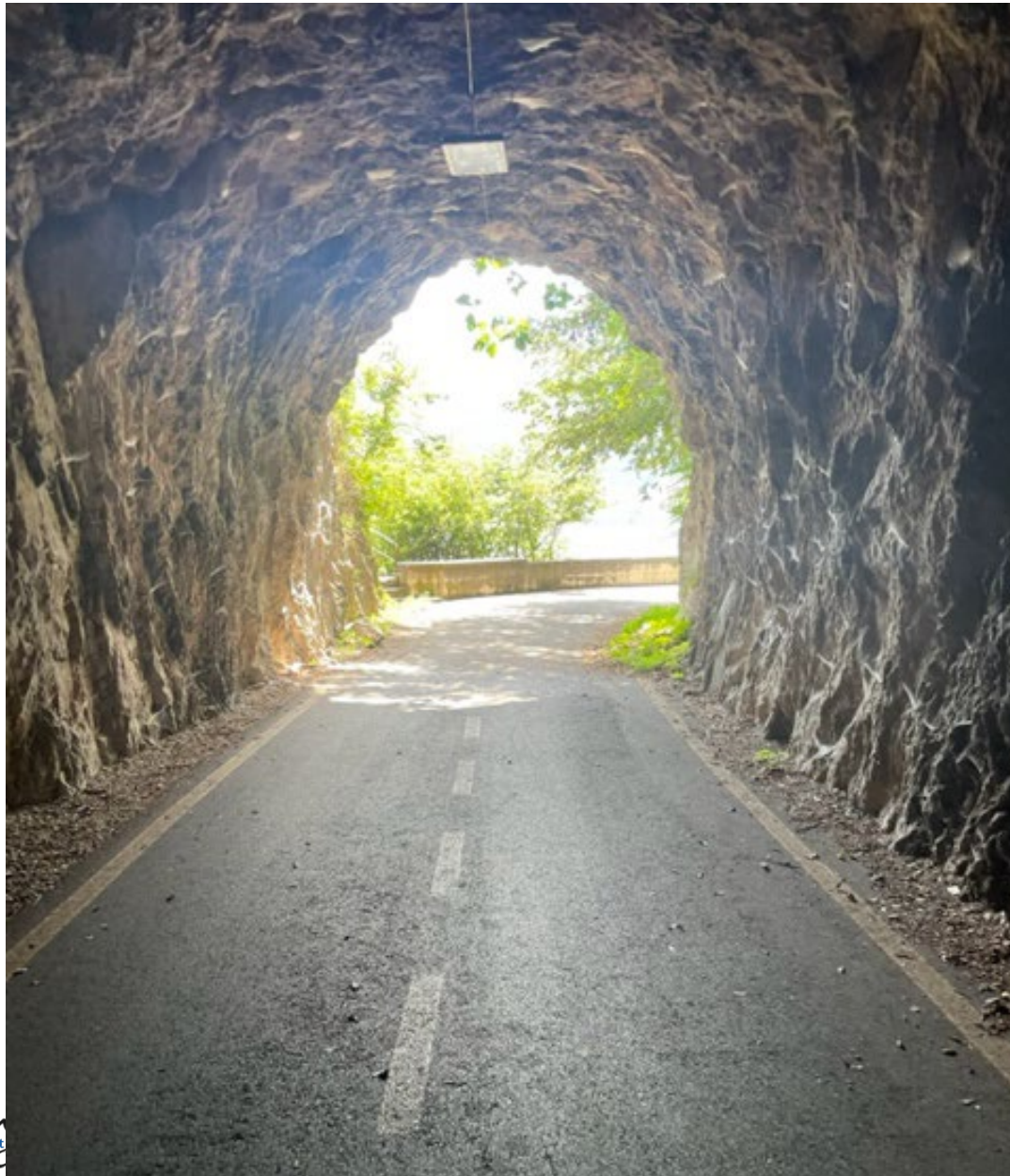
# Going non-linear – Price-responsive demands



- Demand function is calibrated to replicate the demand level
- Revenue = cost + profit
- A carbon tax
  - Reduces quantity
  - Increases price
- Distributional implications
  - Decreases **production cost**
  - Decreases **producer rent**
  - Decreases **consumer rent**
  - Generates a **tax revenue**
  - ➔ **can be redistributed**

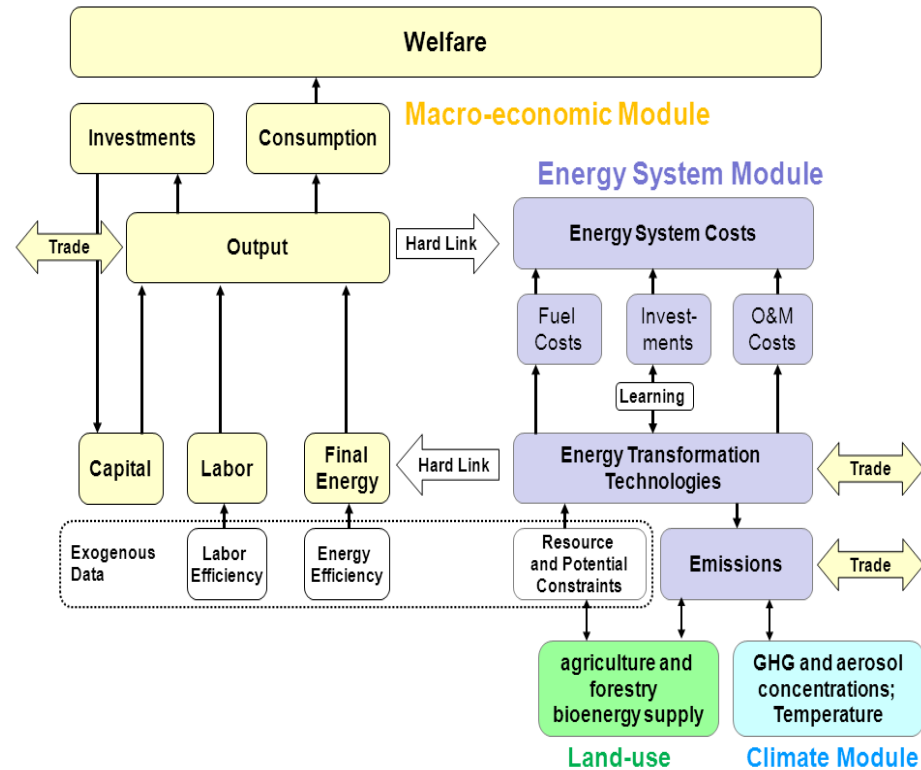
# There is light at the end of tunnel

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# From partial to general equilibrium

- Where does the finance come from?
- $GDP = C + I + ESC$
- $W = \int_{t_0}^{t_1} e^{-\rho t} U(C/Pop) C$
- What is energy used for?
- $GDP = f_{CES}(K, L, FE)$





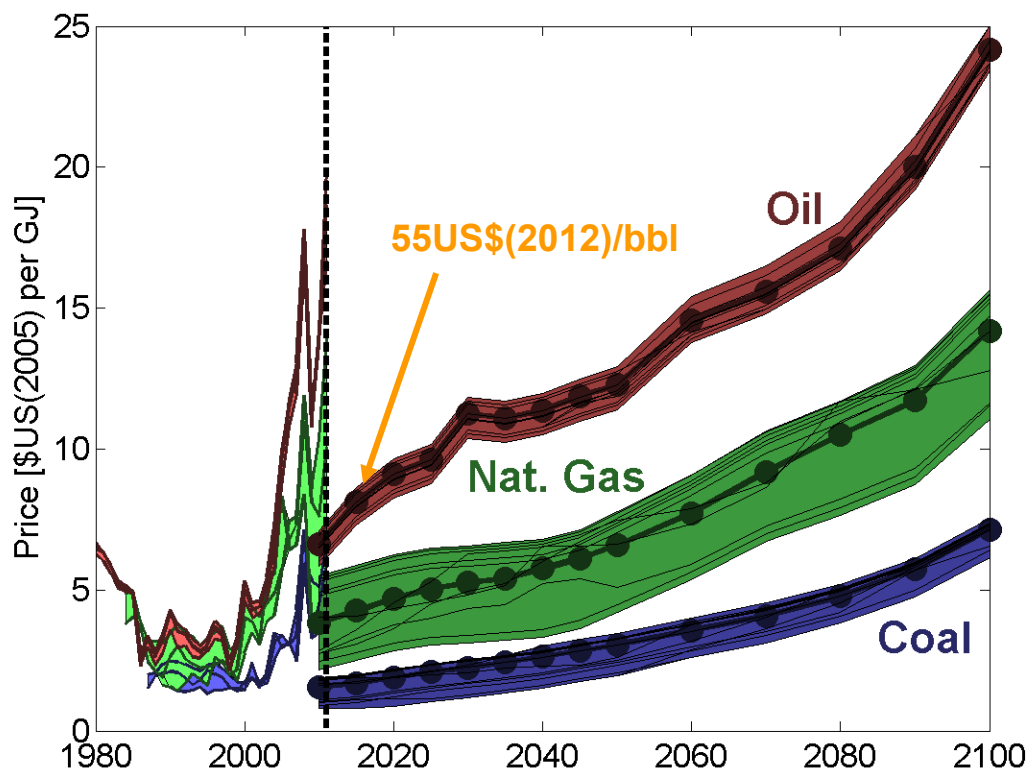
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# Climate Change Mitigation and Fossil Fuels

## Distributional Impacts and Political Economy

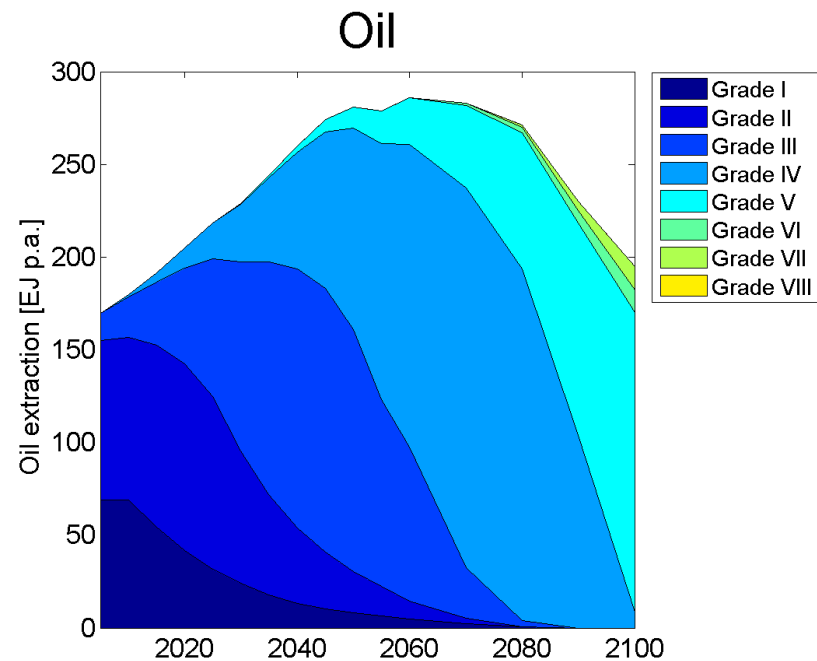


# Climate policies and fossil fuel markets

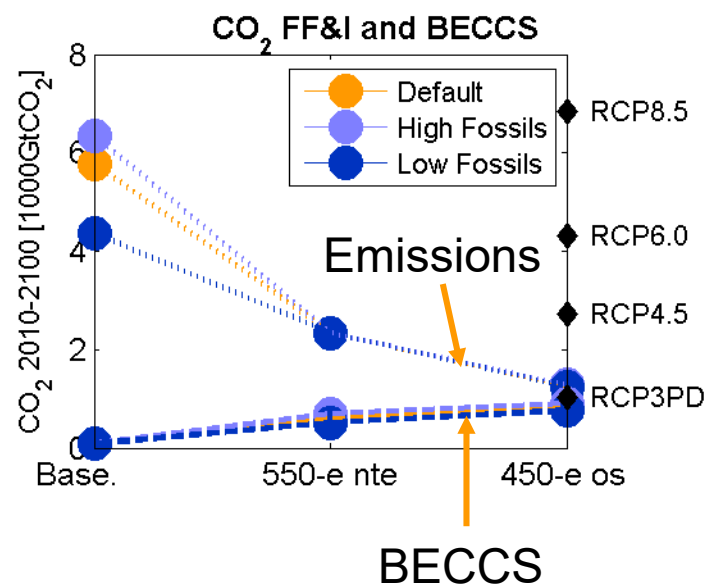


Historic data from BP (2012)

Note: BP reports gas and coal prices only for importing countries



# Climate policies and fossil fuel markets

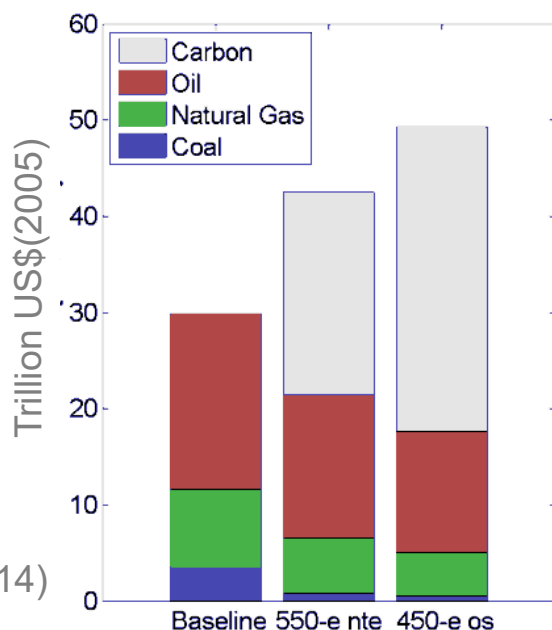


# Climate policies and fossil fuel markets

Discount Rate: 5%/yr

Net Present Value  
tril. US\$(2005)

<b>GDP</b>	<b>1539</b>
<b>GDP Change</b>	<b>-16    -30</b>



Bauer et al. (2014)

- Climate policies reduce GDP
- Fossil fuel owners loose
  - Oil: price effect
  - Coal: quantity effect
- Carbon pricing revenue can compensate losses

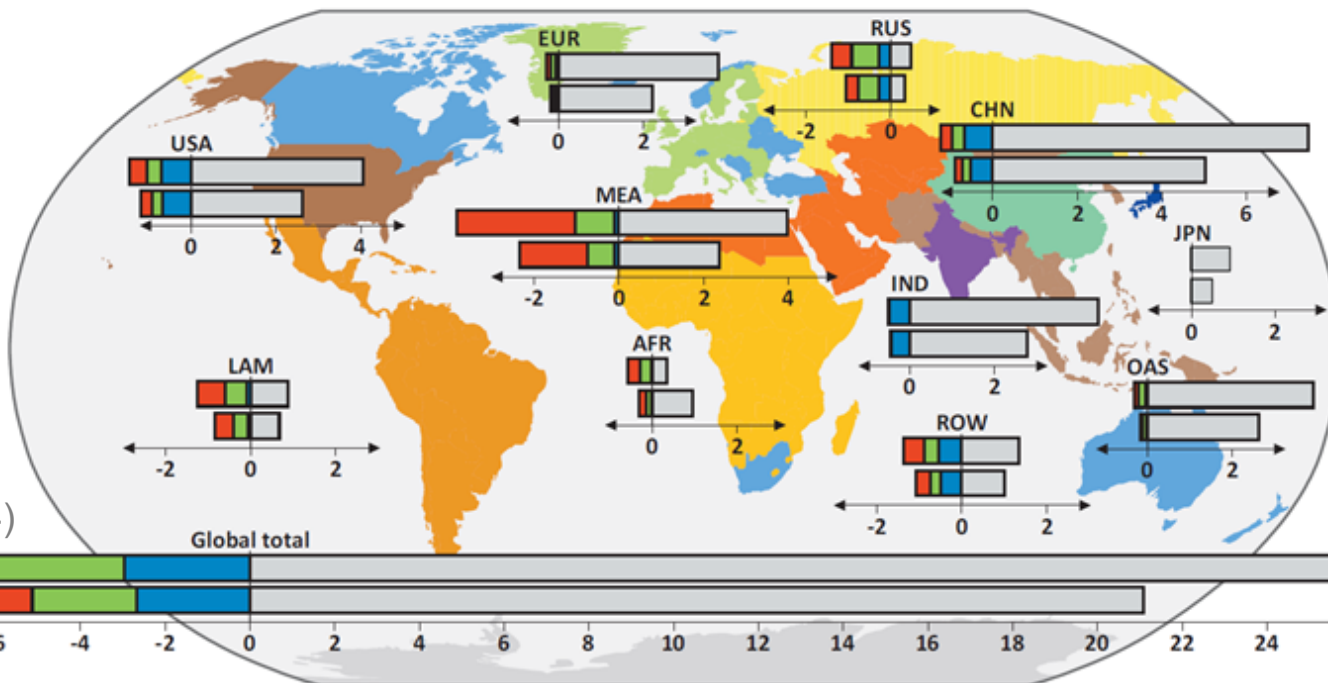
C-price US\$/tCO <sub>2</sub>	Coal 93tCO <sub>2</sub> /TJ	Oil 73tCO <sub>2</sub> /TJ	Gas 55tCO <sub>2</sub> /TJ
	US\$/GJ	US\$/GJ	US\$/GJ
150	16	23	13
<b>50</b>	<b>6.8</b>	<b>15.7</b>	<b>7.8</b>
20	3.9	13.5	6.1
0	2	12	5

# Coal price is currently in huge turmoil (US\$/ton)



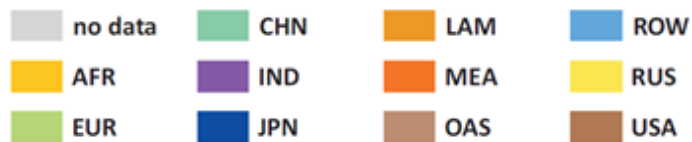
source: tradingeconomics.com

# Climate policies and fossil fuel markets

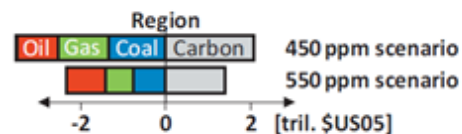


Based on  
Bauer et al. (2014)

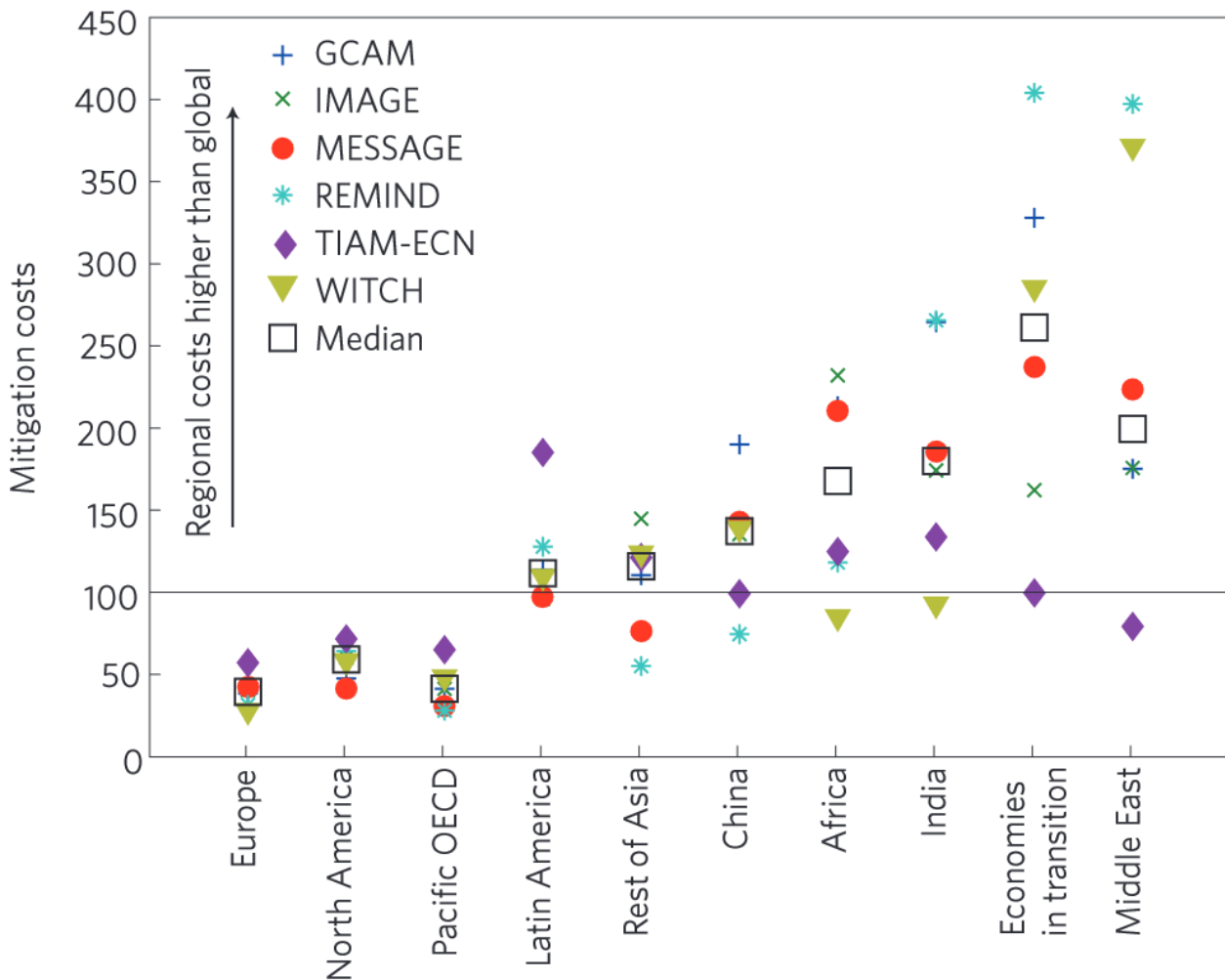
## REMIND regions



## Change in NPV of rent

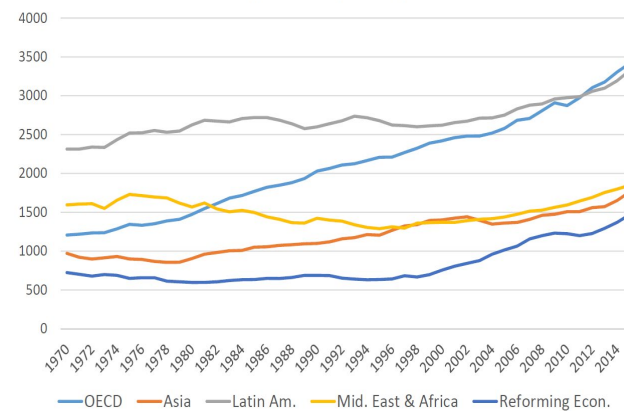


# Short note on regional mitigation costs



## Remember from the intro slides

Carbon productivity in US\$ per tCO<sub>2</sub>



Tavoni et al. (2015)

<http://www.worldscientific.com/doi/abs/10.1142/S2010007813400095>

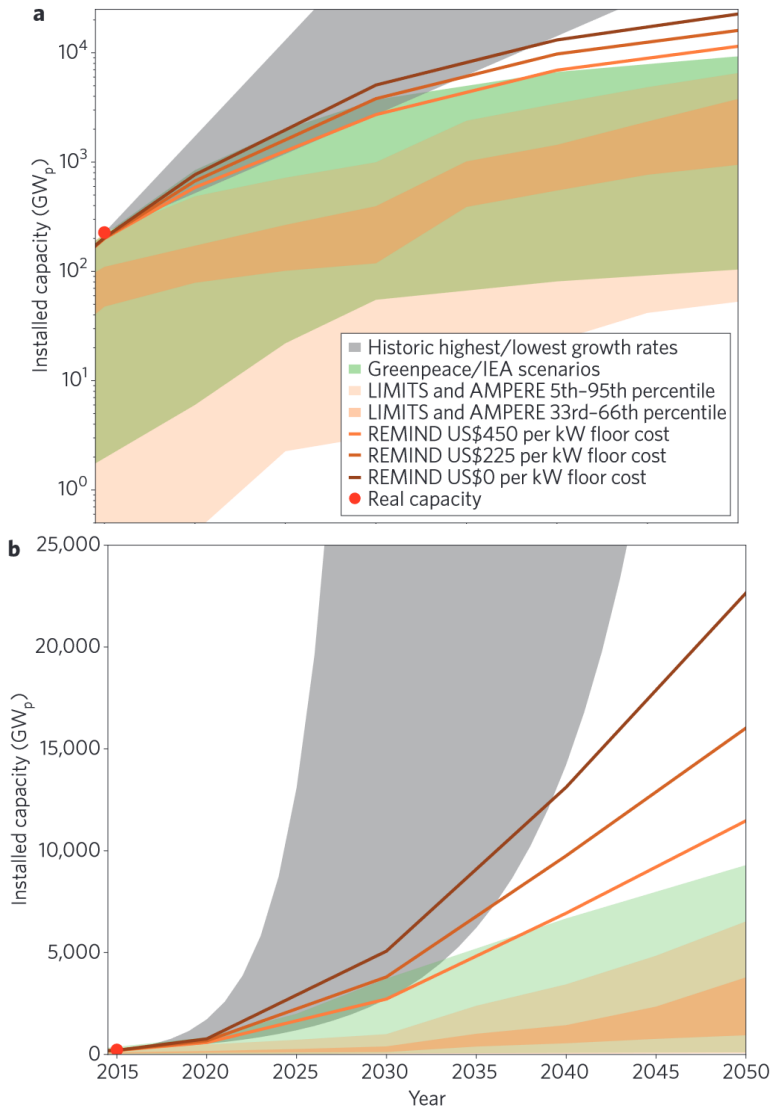
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# Endogenizing Technological Change

## Rushing down the Learning Curve

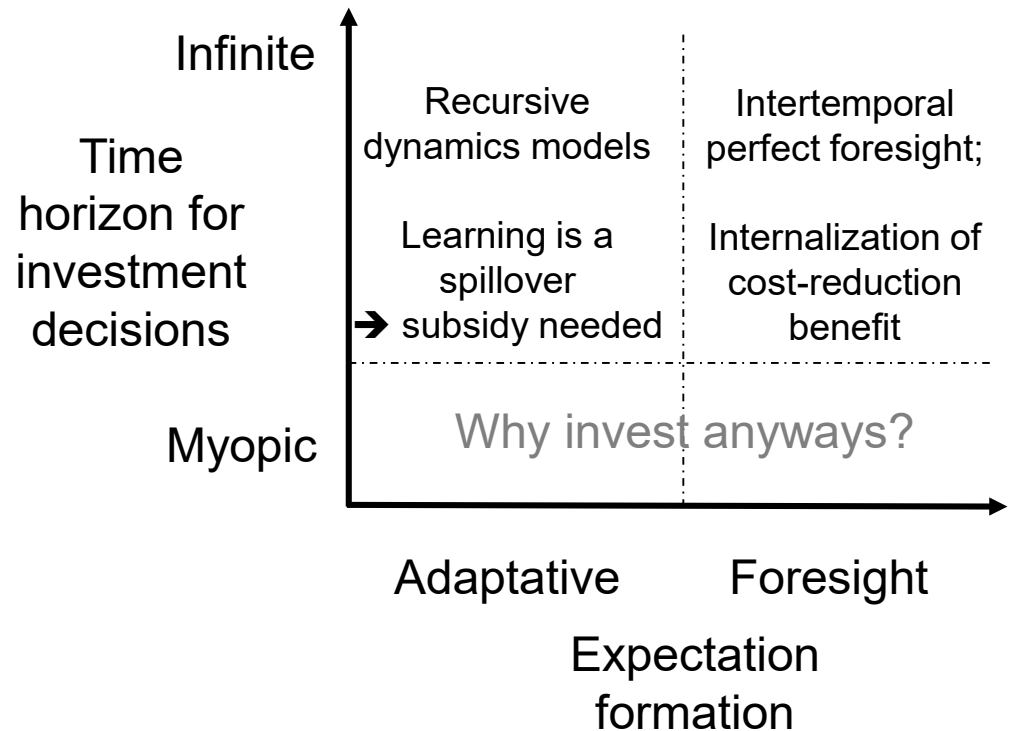


# Endogenous Technology Change – The Learning Curve Approach



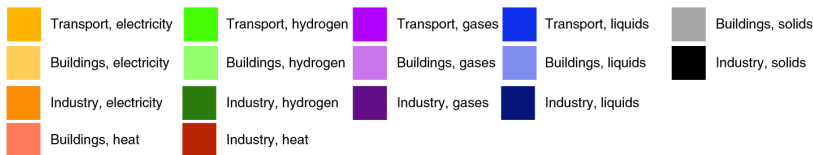
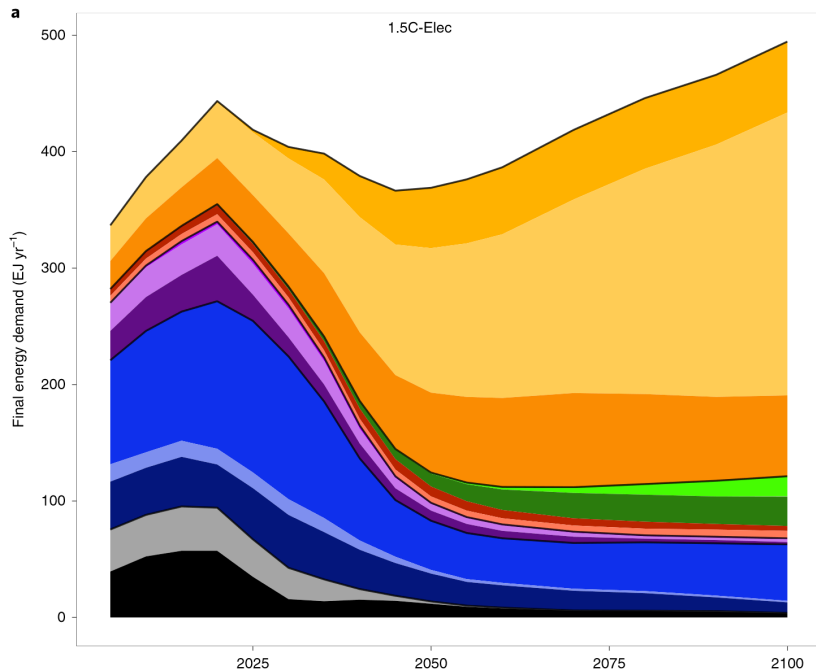
Learning curves can be implemented and solved by:

- Non-linear optimization
- Mixed-Integer Programming

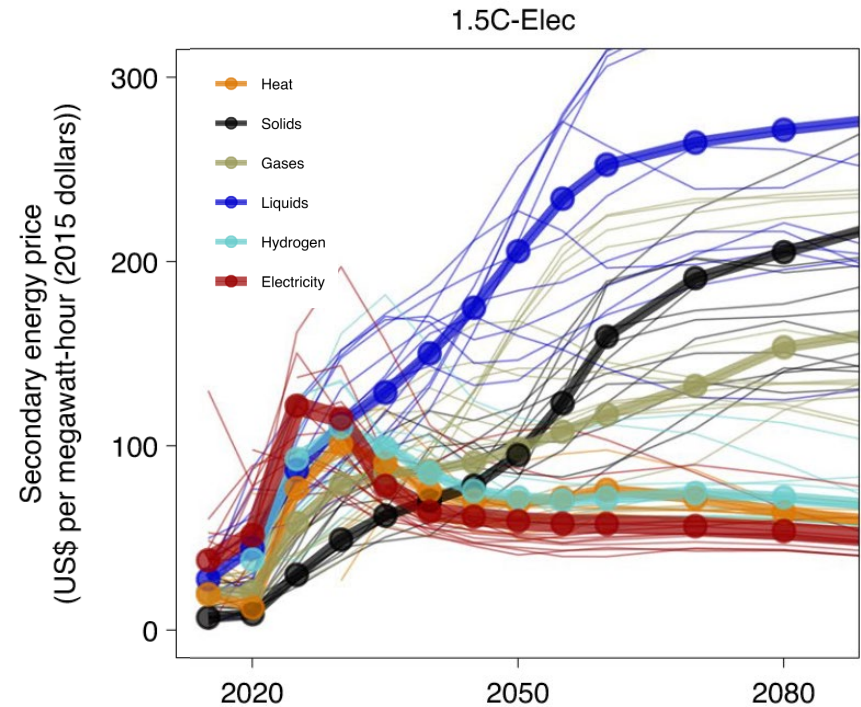


Creutzig et al (2018)  
<https://www.nature.com/articles/nenergy2017140>

# Endogenous Technology Change – The Learning Curve Approach



Luderer et al. (2021) <https://www.nature.com/articles/s41560-021-00937-z>

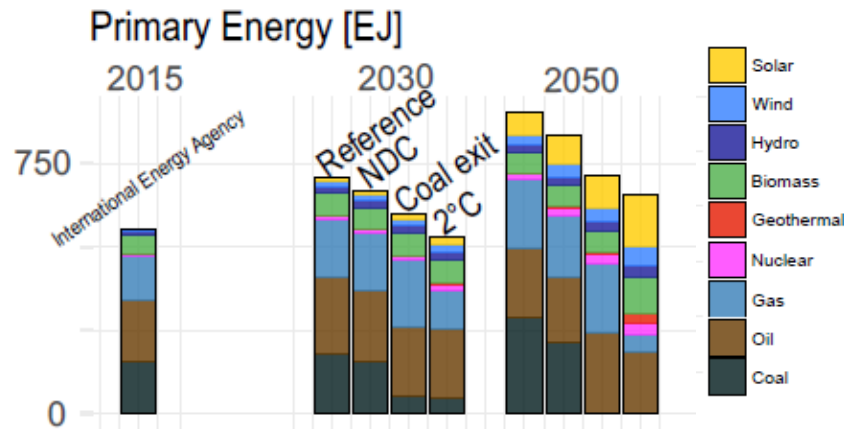


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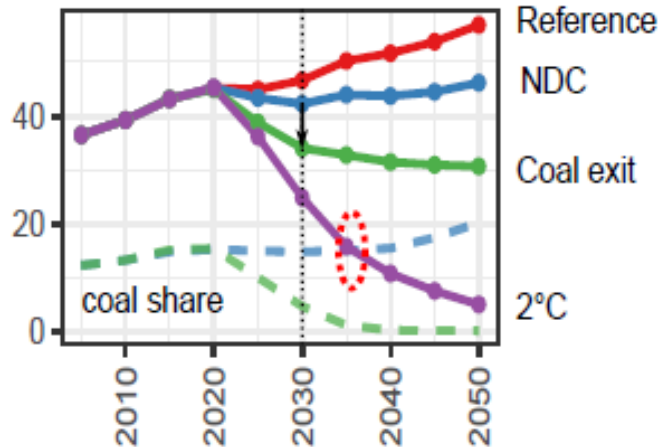
# Air pollution and health impacts driven by IAM results

# Health and environmental effects of coal phase out

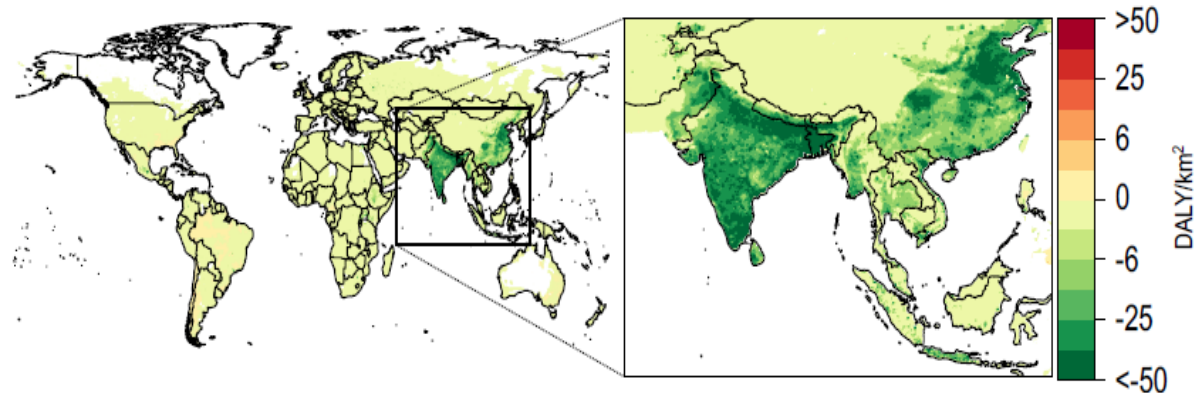


**Reference:** no policy case  
**NDC:** policy evaluation of NDCs  
**Coal exit:** Policy evaluation of coal phase-out from 2°C scenario  
**2°C:** policy optimization

## Global CO<sub>2</sub> emissions in GtCO<sub>2</sub>



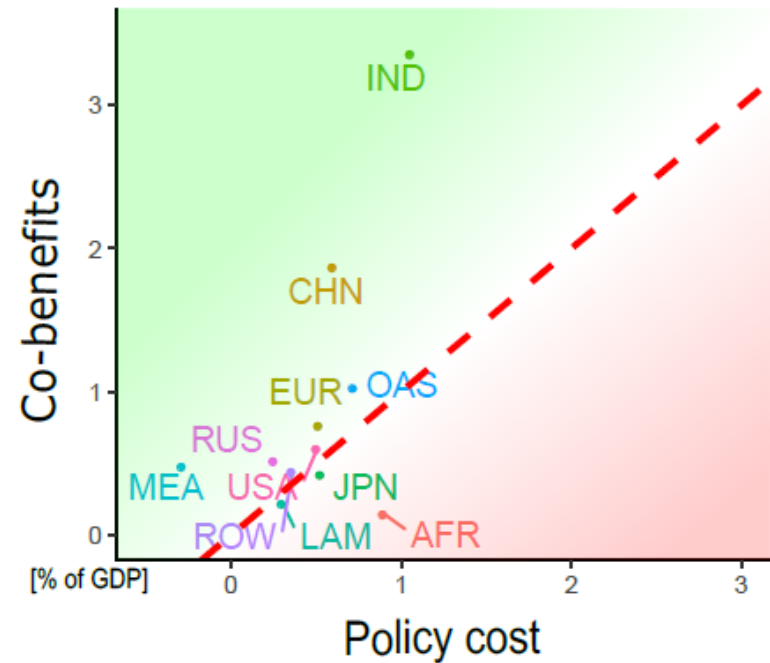
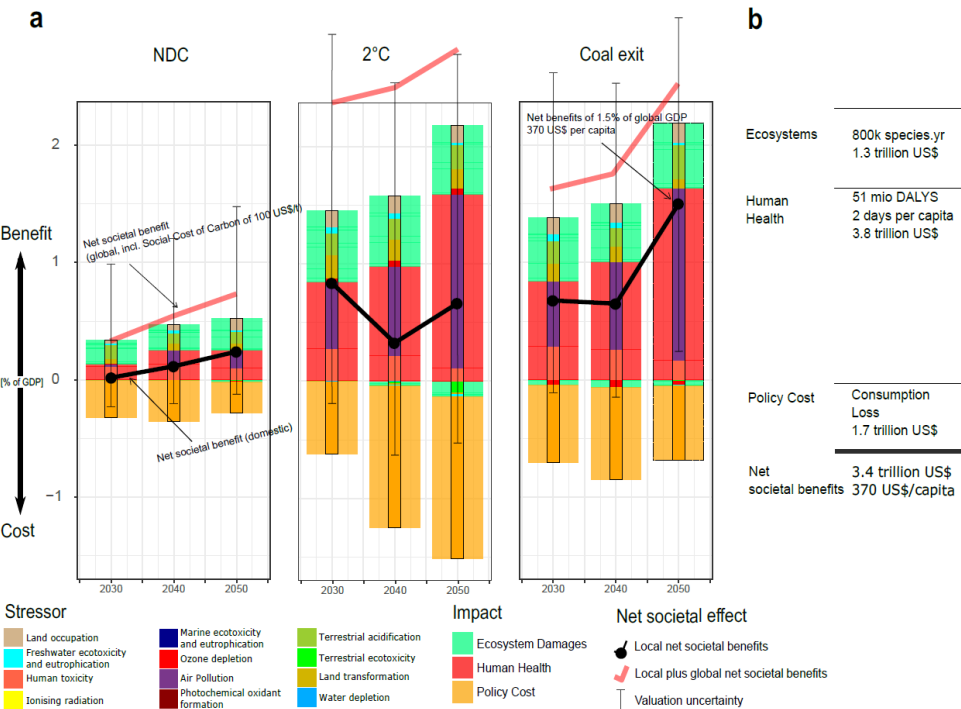
## Health effects from „Coal Exit“ due to reduced air pollution



# Health and environmental effects: global and regional effects

## Global perspective [based on current values]

## Regional perspective [based on net present value in 2050]



Rauner et al. (2020)

<https://www.nature.com/articles/s41558-020-0728-x>





Madonna del Ghisallo  
Patrona dei Ciclisti

